



## **Conference Proceedings**

*1998 International Conference on*

# **Mathematical Methods in Electromagnetic Theory**

**MMET 98**

Volume 1

Kharkov, Ukraine

*June 2-5, 1998*

*Organized and sponsored by*

IEEE AP/MTT/ED/AES Societies East Ukraine Joint Chapter

*in cooperation with*

Ukrainian URSI Commission "B"

Institute of Radiophysics & Electronics  
of the National Academy of Sciences of Ukraine

Institute of Radio Astronomy  
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*We wish to thank the following co-sponsors for their contribution  
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US Office of Naval Research European Office  
INTAS – International Association

1998 International Conference on Mathematical Methods in Electromagnetic Theory

IEEE Catalog Number:	98EX114	
ISBN:	0-7803-4360-3	Softbound Edition
	0-7803-4361-1	Microfiche Edition
Library of Congress:	97-80498	

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## MODEL OF SIGNALS FOR DIGITAL ANTENNA ARRAY WITH MUTUAL COUPLING ON THE BASIS OF FACE-SPLITTING MATRICES PRODUCT

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When considering the multicoordinate digital antenna arrays (DAA) with mutual coupling of channels there arises a problem of compact matrix record of the responses of reception channels. For the solution of the given problem it is proposed to operate with a special type of the product of matrices, named as "face-splitting" ( $a \square b = [a_{ij} \cdot B_i]$ ) and "transposed face-splitting" product (TFSP) ( $a \blacksquare b = [a_{ij} \cdot B_j]$ ), respectively, [1].

With the aid of TFSP it is possible to obtain the variant of analytical model of two-coordinate DAA with mutual coupling:

$$U = (F \otimes W)(Q \blacksquare V) \cdot A, \quad (1)$$

where  $U$  is a block-vector of voltages of the responses of DAA channels,  $Q$ ,  $V$  is the  $R \times M$  matrix of the directivity characteristics of primary channels in azimuth and elevation angle planes,

$$Q = \begin{bmatrix} Q_1(x_1) & Q_1(x_2) & \cdots & Q_1(x_M) \\ Q_2(x_1) & Q_2(x_2) & \cdots & Q_2(x_M) \\ \vdots & \vdots & \vdots & \vdots \\ Q_R(x_1) & Q_R(x_2) & \cdots & Q_R(x_M) \end{bmatrix}, \quad V = \begin{bmatrix} V_1(y_1) & V_1(y_2) & \cdots & V_1(y_M) \\ V_2(y_1) & V_2(y_2) & \cdots & V_2(y_M) \\ \vdots & \vdots & \vdots & \vdots \\ V_R(y_1) & V_R(y_2) & \cdots & V_R(y_M) \end{bmatrix};$$

$$Q \blacksquare V = \begin{bmatrix} \begin{bmatrix} Q_1(x_1) & \vdots \\ V_1(y_1) & \vdots \\ V_R(y_1) \end{bmatrix} & \begin{bmatrix} Q_1(x_2) & \vdots \\ V_1(y_2) & \vdots \\ V_R(y_2) \end{bmatrix} & \cdots & \begin{bmatrix} Q_1(x_M) & \vdots \\ V_1(y_M) & \vdots \\ V_R(y_M) \end{bmatrix} \\ \begin{bmatrix} Q_2(x_1) & \vdots \\ V_1(y_1) & \vdots \\ V_R(y_1) \end{bmatrix} & \begin{bmatrix} Q_2(x_2) & \vdots \\ V_1(y_2) & \vdots \\ V_R(y_2) \end{bmatrix} & \cdots & \begin{bmatrix} Q_2(x_M) & \vdots \\ V_1(y_M) & \vdots \\ V_R(y_M) \end{bmatrix} \\ \vdots & \vdots & \vdots & \vdots \\ \begin{bmatrix} Q_R(x_1) & \vdots \\ V_1(y_1) & \vdots \\ V_R(y_1) \end{bmatrix} & \begin{bmatrix} Q_R(x_2) & \vdots \\ V_1(y_2) & \vdots \\ V_R(y_2) \end{bmatrix} & \cdots & \begin{bmatrix} Q_R(x_M) & \vdots \\ V_1(y_M) & \vdots \\ V_R(y_M) \end{bmatrix} \end{bmatrix};$$

$F$ ,  $W$  is the  $R \times R$  matrix of mutual coupling,

$$F = \begin{bmatrix} 1 & F_{12} & \dots & F_{1R} \\ F_{21} & 1 & \dots & F_{2R} \\ \vdots & \vdots & \ddots & \vdots \\ F_{R1} & F_{R2} & \dots & 1 \end{bmatrix}, \quad W = \begin{bmatrix} 1 & W_{12} & \dots & W_{1R} \\ W_{21} & 1 & \dots & W_{2R} \\ \vdots & \vdots & \ddots & \vdots \\ W_{R1} & W_{R2} & \dots & 1 \end{bmatrix}, \quad |F_{nm}| < 1, \quad |W_{nm}| < 1;$$

$A = [\hat{a}_1 \quad \hat{a}_2 \quad \dots \quad \hat{a}_M]^T$  is the vector of complex amplitudes of signals of M sources.

With the aid of identities [ 2 ]:

$$(F \otimes W)(Q \blacksquare V) = (F \cdot Q) \blacksquare (W \cdot V),$$

one can obtain that

$$U = P \cdot A, \text{ where } P = (F \cdot Q) \blacksquare (W \cdot V) \tag{2}$$

By using the method of maximum likelihood, an estimation of parameters of M sources of signals of two-coordinate DAA it is possible to be carried out, by a minimization of a functional not differing in form from that used in one-coordinate case. Indeed, it is possible to write down:

$$L = \{U - P \cdot A\}^* \{U - P \cdot A\} = \min$$

The measuring procedure in the wo-coordinate variant is reduced to the minimization of expression:

$$L = \text{tr} [G \cdot R], \text{ where } G = P \cdot (P^* \cdot P)^{-1} \cdot P^*, \quad R = U \cdot U^*.$$

With the account of (2), on the basis of matrix Neudecker derivative [3] an information fisher's block-matrix describing the accuracy of joint estimation of angular coordinates is obtained [4]:

$$I = \frac{1}{\sigma^2} \cdot \begin{bmatrix} P^T \cdot P & \vdots & (A^* \otimes P^T) \cdot \frac{\partial P}{\partial Y} \\ \dots\dots\dots & \vdots & \dots\dots\dots \\ \left(\frac{\partial P}{\partial Y}\right)^T \cdot (A \otimes P) & \vdots & \left(\frac{\partial P}{\partial Y}\right)^T \cdot (AA^* \otimes I_{RR}) \cdot \frac{\partial P}{\partial Y} \end{bmatrix},$$

where  $\frac{\partial P}{\partial Y}$  is the Neudecker derivative of the matrix P by the vector Y formed by unknown estimations of angular coordinates of M sources;  $I_{RR}$  is the identity matrix of dimension  $R \times R$ ;  $\otimes$  is the symbol of Kronecker-products of matrices.

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